

## 1.1 Problems NS-1

### Topic of this homework:

Introduction to Matlab/Octave (see the Matlab or Octave tutorial for help)

Deliverables: Report with charts and answers to questions.

### Plotting complex quantities in Octave/Matlab

**Problem # 1:** Consider the functions  $f(s) = s^2 + 6s + 25$  and  $g(s) = s^2 + 6s + 5$ .

– 1.1: Find the zeros of functions  $f(s)$  and  $g(s)$  using the command `roots()`.

**Ans:**

– 1.2: Show the roots of  $f(s)$  as red circles and of  $g(s)$  as blue plus signs.

The  $x$ -axis should display the real part of each root, and the  $y$ -axis should display the imaginary part. Use `hold on` and `grid on` when plotting the roots.

**Ans:**

– 1.3 Give your figure the title “Complex Roots of  $f(s)$  and  $g(s)$ .” Label the  $x$ - and  $y$ -axes “Real Part” and “Imaginary Part.” Hint: Use `xlabel`, `ylabel`, `ylim([-10 10])`, and `xlim([-10 10])` to expand the axes.

**Problem # 2:** Consider the function  $h(t) = e^{j2\pi ft}$  for  $f = 5$  and  $t = [0:0.01:2]$ .

– 2.1: Use `subplot` to show the real and imaginary parts of  $h(t)$ .

Make two graphs in one figure. Label the  $x$ -axes “Time (s)” and the  $y$ -axes “Real Part” and “Imaginary Part.”

**Ans:**

– 2.2: Use `subplot` to plot the magnitude and phase parts of  $h(t)$ .

Use the command `angle` or `unwrap(angle())` to plot the phase. Label the  $x$ -axes “Time (s)” and the  $y$ -axes “Magnitude” and “Phase (radians).”

**Ans:**

**Prime numbers, infinity****Problem # 3: Prime numbers**

– 3.1: Use the Matlab/Octave function `factor` to find the prime factors of 123, 248, 1767, and 999,999.

**Ans:**

– 3.2: Use the Matlab/Octave function `isprime` to determine whether 2, 3, and 4 are prime numbers. What does the function `isprime` return when a number is prime or not prime? Why?

**Ans:**

– 3.3: Use the Matlab/Octave function `primes` to generate prime numbers between 1 and  $10^6$ . Save them in a vector `x`. Plot this result using the command `hist(x)`.

**Ans:**

– 3.4: Now try `[n,bincenters] = hist(x)`. Use `length(n)` to find the number of bins.

**Ans:**

– 3.5: Set the number of bins to 100 by using an extra input argument to the function `hist`. Show the resulting figure, give it a title, and label the axes. Hint: `help hist` and `doc hist`.

**Ans:**

**Problem # 4: Very large primes on Intel computers.**

– 4.1: Find the largest prime number  $\pi_{\max}$  that can be stored on an Intel 64-bit computer; Hint: As explained in the Matlab/Octave command `help flintmax`.

The largest positive integer is  $2^{53}$ ; however, the largest unsigned integer that can be factored is at least  $2^{54}$ . Explain the logic of your answer. Hint: `help isprime()`.

**Ans:**

**Problem # 5: We are interested in primes that are greater than  $\pi_{\max}$ .**

– 5.1: How can you find them on an Intel computer (i.e., one using IEEE floating point)? Hint: Consider a sieve that contains only odd numbers, starting from 3 (not 2). Since every prime number greater than 2 is odd, there is no reason to check the even numbers.  $n_{\text{odd}} \in \mathbb{N}/2$  contain all the primes other than 2.

**Ans:**

**Special functions in Octave/Matlab and infinity ( $\infty$ )****Problem # 6: `Inf`, `NaN`, and logarithms in Octave/Matlab.**

– 6.1: Try `1/0` and `0/0` in the Octave/Matlab command window. What are the results? What do these “numbers” mean in Octave/Matlab? **Ans:**

– 6.2: Try  $\log(0)$ ,  $\log_{10}(0)$ , and  $\log_2(0)$  in the command window.

In Matlab/Octave, the natural logarithm  $\ln(\cdot)$  is computed using the function `log`. Functions  $\log_{10}$  and  $\log_2$  are computed using `log10` and `log2`. **Ans:**

– 6.3: Try  $\log(1)$  in the command window. What do you expect for  $\log_{10}(1)$  and  $\log_2(1)$ ?

**Ans:**

– 6.4: Try  $\log(-1)$  in the command window. What do you expect for  $\log_{10}(-1)$  and  $\log_2(-1)$ ?

**Ans:**

– 6.5: Explain how Matlab/Octave arrives at the answer in problem 6.4. Hint:  $-1 = e^{i\pi}$ .

**Ans:**

– 6.6: Try  $\log(\exp(j*\text{sqrt}(\text{pi})))$  (i.e.,  $\log e^{j\sqrt{\pi}}$ ) in the command window. What do you expect?

**Ans:**

– 6.7: What does “inverse” mean in this context? What is the inverse of  $\ln f(x)$ ?

**Ans:**

– 6.8: What is a decibel? (Look up decibels on the internet.)

**Ans:**

**Problem # 7:** The following identity is interesting. Can you find a proof?

$$\begin{aligned}
 1 &= 1^2 \\
 1 + 3 &= 2^2 \\
 1 + 3 + 5 &= 3^2 \\
 1 + 3 + 5 + 7 &= 4^2 \\
 1 + 3 + 5 + 7 + 9 &= 5^2 \\
 &\vdots \\
 \sum_{n=0}^{N-1} 2n + 1 &= N^2.
 \end{aligned}$$

– 7.1: Can you find a proof?

**Ans:**